

Q1*. Let $x_0 \in \mathbb{R}$, $\zeta \in \mathbb{R} \cup \{\pm\infty\} = [-\infty, \infty]$ and
 $f: \mathbb{R} \setminus \{x_0\} \rightarrow \mathbb{R}$. Show that

$$\lim_{x \rightarrow x_0} f(x) = \zeta \Leftrightarrow \lim_{x \rightarrow x_0^-} f(x) = \zeta = \lim_{x \rightarrow x_0^+} f(x)$$

and hence that $\lim f(x)$ not exist in $[-\infty, \infty]$
if $\lim_{x \rightarrow x_0^-} f(x) \neq \lim_{x \rightarrow x_0^+} f(x)$.

Q2* = q10(b) of Bartle § 4.1

Q3 = q14
Q4* = q15 } of Bartle § 4.1.

Q5 = q16

Q6* = q1(b) of Bartle § 4.2

Q7* = q2(d).

Q8* (cf. q3)

Use the computation rules to calculate

$$\lim_{x \rightarrow 0} \frac{\sqrt{1+2x} - \sqrt{1+3x}}{x+2x^2} = -\frac{1}{2}$$

(Quite difficult to check with $\epsilon-\delta$!
- not required at this time).

